EXPERIMENTAL EVALUATION OF NONLINEAR INDICES FOR ULTRASOUND TRANSDUCER CHARACTERIZATIONS

BY

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THESIS

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